**SINGLE-STUB TUNING**

The basic idea is to connect a line stub in parallel (shunt) or series a distance $d$ from the load so that the imaginary part of the load impedance will be canceled.

**Shunt-stub:** Select $d$ so that the admittance $Y$ looking toward the load from a distance $d$ is of the form $1/Y$. Then the susceptance $B$ is $Y$, and the new load is of $Z_0 = 300$.

**Series-stub:** Select $d$ so that the susceptance $B$ looking toward the load from a distance $d$ is of the form $B/Y$. Then the admittance $Y$ is $B$, and the new load is of $Z_0 = 300$.

---

**FINDING A STUB LENGTH**

Example: Find the lengths of open and shunted short stubs to match an admittance of $Y = j/2$. The admittance of an open stub (zero length) is $Y_0$, the point is located at the left end of the Smith Chart $r = 0$. We proceed clockwise around the Smith chart, i.e., away from the end of the stub, to the $Y = j/2$, (the value needed to match $Y = j/2$). The difference in the starting point and the end point on the wavelength scale is the length of the stub in wavelengths. This length of a shunted stub is the same manner but with the starting point at $Z_0$.

---

**TRANSMISSION COEFFICIENT**

The transmission coefficient is the ratio of total voltage to the forward-traveling voltage, a value ranging from 0 to 2.

$$\tau = \frac{V_{out}}{V_{in}} = 1 + \rho$$

**CIRCULATOR**

The circulator is a 3-port network that can be electrically connected to the antenna as shown in the figure. The circulator may be protected by a matched load. With a load at 2, any power reflected at the load at the load resistance at port 3. A 3-port is both lossless and reciprocal, so the reciprocal.

---

**MODELING MAXWELL'S EQUATIONS**

This is a model of a wave, analogous to a transmission line model.

$$L = \mu \cdot 1/m$$

**MODULATED WAVE**

Suppose we have a disturbance composed of two frequencies:

$$\sin \left( \omega_0 + \omega \cdot t - B \cdot t \right)$$

and

$$\sin \left( \omega_0 + \omega \cdot t - B \cdot t \right)$$

where $\omega_0$ is the average frequency and $B_0$ is the average phase.

Using the identity

$$2 \cos \left( \frac{4 + B}{2} \right) \sin \left( \frac{4 + B}{2} \right) = \sin A \cdot \cos A + \cos A \cdot \sin B$$

The combination (sum) of these two waves is

$$2 \cos \left( \frac{4 + B}{2} \right) \sin \left( \frac{4 + B}{2} \right)$$

The envelope moves at the group velocity, see p. 7.

---

**VELOCITY**

The velocity of propagation of a wave approaches the speed of light since this information can not exceed the speed of light.

$$v = \alpha / \beta$$

**Phase Velocity**

The velocity of propagation of a TEM wave may also be referred to as the phase velocity. The phase velocity of a TEM wave in perfect conductor may be described by:

$$v_p = c \sin \phi = \frac{c}{\sqrt{\mu_0 \varepsilon_0}}$$

where:

$$\delta = \phi$$

- $c$ = speed of light $2.998 \times 10^8$ m/s
- $\lambda_0$ = wavelength in the material [m]
Comparing Microstrip and CPW Performance

By building a better electromagnetic (EM) simulation model, which includes the effects of a PCB’s metal surface roughness, microstrip and coplanar waveguide, circuits can be closely compared to find the best fit for different applications.

Matching a microwave transmission-line technology to an application requires careful consideration of more than a few factors. Depending on the requirements of an application, high-frequency circuit designers may be concerned with loss budgets, propagation mode issues, radiation losses and electromagnetic interference (EMI), and even the printed-circuit-board (PCB) assembly logistics and the relative difficulty of adding components to a PCB. Microstrip has been one of the most popular microwave transmission-line formats for decades and is well characterized. Coplanar waveguide (CPW) transmission lines have also been used extensively in microwave PCB applications, although they are not as well understood as microstrip lines. Typically, conductor-backed coplanar waveguide (CBCPW) circuits are often used in conjunction with microstrip in microwave circuit designs. A common approach is the use of CBCPW in the circuit’s signal launch area, transitioning to microstrip for the remainder of the circuit to enable simple component placement and PCB assembly.

To help designers understand differences between microstrip and CPW transmission-line approaches, measurement data from different test circuits fabricated with the same, well-known commercial substrate material will be compared. Further analysis will be performed with the aid of electromagnetic (EM) models and EM simulation software. The software modeling will help validate the measured results and also show how effective software modeling can alleviate concerns, when using new transmission-line approaches and/or circuit topologies.

Microstrip and CPW formats are often selected over other high-frequency transmission-line options, such as stripline, due to their simplicity. Stripline can deliver excellent high-frequency performance, with good noise immunity and isolation between adjacent circuit traces. But it is also more difficult and expensive to fabricate than microstrip or CPW. Stripline is essentially a flat metal transmission line between two ground planes, with the ground planes separated by a dielectric substrate material. The width of the transmission line, the thickness of the substrate, and the relative dielectric constant of the substrate material determine the characteristic impedance of the transmission line. Difficulties with stripline

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hybrid transverse-magnetic modes are also possible with microstrip, but these modes are sometimes the result of undesired spurious wave propagation. In general, CBCPW circuits offer propagation behavior similar to that of microstrip circuits.

For both microstrip and CBCPW circuits, spurious parasitic wave propagation can be a problem. As a general rule, the circuit geometry (that is its cross-sectional features) for either transmission-line approach should be less than 45° long at the highest operating frequency of interest. For microstrip, the circuit parameters of concern include the thickness of the substrate (that is the distance between the signal and ground planes) and the width of the signal conductor (transmission line width). For CBCPW, attention must be paid to those two parameters, as well as to the distance between the GSG spacing on the coplanar layer.

For proper grounding, CBCPW circuits employ vias to connect the top-layer coplanar ground planes and the bottom-layer ground plane. The placement of these vias can be critical for achieving the desired impedance and loss characteristics, as well as for suppressing parasitic wave modes. When grounding vias are effectively positioned in a CBCPW circuit, a much thicker dielectric substrate can be used at higher frequencies than would be possible for a microstrip circuit at the same frequencies. A review of the practical tradeoffs of via placement for CBCPW circuits is available in the literature. Figure 2 offers an overview of signal loss ($S_{21}$) performance for microstrip, coplanar-launched microstrip, and CBCPW circuits fabricated on 30-mil-thick RO4350B™ circuit-board material from Rogers Corp.

GCPWG refers to a grounded coplanar waveguide and is actually the same configuration as CBCPW. The top ground microstrip configuration is essentially a coplanar-launched microstrip circuit – a microstrip circuit with a CBCPW configuration in the connector signal launch area. The curve-fit data for microstrip and coplanar-launched microstrip are taken from the literature. The traces reveal some interesting traits to consider for the different transmission lines. For example, CBCPW typically suffers higher loss than microstrip or coplanar-launched microstrip. The GSG configuration of the CBCPW coplanar layer exhibits higher conductor loss than microstrip-based circuits. Still, the loss for CBCPW follows a constant slope, while the loss curves for microstrip and coplanar-launched microstrip undergo slope transitions at approximately 27 and 30 GHz, respectively. These loss transitions are associated with radiation losses. With proper spacing and via spacing, CBCPW can be fabricated with minimal radiation loss.

In wideband applications, dispersion can be important. Microstrip transmission lines are dispersive by nature: the phase velocity for EM waves is different in the air above the signal conductor than through the dielectric material of the substrate. CBCPW circuits can achieve much less dispersion when there is tight coupling at the GSG interfaces on the coplanar layer, since more of the E-field occurs in air to reduce the effective inhomogeneity of wave travel through different media.

Using proper design techniques, CBCPW circuits can achieve a much wider range of impedances than microstrip circuits. In addition, applications where crosstalk may be a concern, circuit performance can benefit from the coplanar ground plane separation of CBCPW’s neighboring signal conductors. Due to their significantly
reduced radiation losses, dispersion and parasitic wave mode propagation. CBCPW circuits are often used at much higher frequencies than microstrip circuits. At millimeter-wave frequencies, for example, it is often that a simple wire-bonded air bridge will be used to connect the ground planes on both sides of the CBCPW signal conductor. The air bridge approach serves as a “trap” for specific frequencies of concern when spurious wave mode propagation is an issue.2

COPPER SURFACE ROUGHNESS

The copper surface roughness of PCB substrates has been known to affect conductor losses as well as the propagation constant of the transmission line.3 The effect on a transmission-line’s propagation constant causes a circuit to have a different “apparent dielectric constant” than expected. Of course, the material parameter is unchanged by the roughness of the material’s metal layer. Rather, the amount of metal surface roughness causes the observed effects by influencing electric field and current flow. As Figure 3 shows,3 the effective dielectric constant can vary widely for the same dielectric substrate when the copper surface roughness is different. The effective dielectric constant increases as the surface roughness of the copper increases, as indicated by copper surfaces with higher root-mean-square (RMS) roughness values.

In addition to observed dielectric constant effects, the surface roughness of a microstrip is known to impact insertion loss performance.3–7 The topology of the circuit may be more or less prone to such copper surface roughness effects, simply due to current and E-field distribution within the circuit. For example, the copper surface roughness has less effect on a tightly coupled CBCPW transmission line than on a microstrip. In a CBCPW circuit, the current and E-field are tightly maintained within the GSG on the coplanar layer. For a microstrip circuit, the field and current move more toward the bottom of the metal, where the roughness lies.

MEASURING DIFFERENCES

All of the circuits evaluated in this article were fabricated on a 254 µm (10-mil) thick RT/duriod® 5880 laminate from Rogers Corp. The same dielectric material was used in all cases, although with different copper types: rolled copper with surface roughness of 0.4 µm RMS, electrodeposited (ED) copper with surface roughness of 1.8 µm RMS, and high-profile ED copper with surface roughness of 2.8 µm RMS. Table 1 provides details on the dimensions of the different circuits, along with their measured characteristic impedances. The nominal circuit dimensions noted in the table are per the circuit design; however, typical PCB fabrication tolerances apply. On the actual circuits, the signal-to-ground spacing for the coplanar layer of the CBCPW and the copper thickness had appreciable circuit-to-circuit variation.

There is also a real-life issue affecting most PCB circuits and especially CBCPW, which can cause more variation in circuit performance due to standard fabrication effects. This is the conductor trapezoidal effect, or “edge profile,” where the PCB conductors are ideally rectangular in a cross-sectional view but the actual circuits are trapezoidal in shape. This can cause the current density in the coplanar GSG area to vary; an ideal rectangular conductor structure will have more current density up the sidewalls of the adjacent conductors in this region, whereas the trapezoidal structure will have more current density at the base (copper-substrate interface). When there is more current density at the base due to the trapezoidal effect, the copper surface roughness will have more influence on losses and the propagation constant. The trapezoidal concerns for CBCPW PCBs are shown in Figure 4.

Figure 5 compares the effective dielectric constants for two different coplanar circuit types and how they are affected by two extreme cases of copper surface roughness. The phase response measurements that were made for one data set of circuits employed a differential phase length method.8 Circuits were made in very close proximity on the same processing panel and the only difference for the two circuits being measured was the physical length of the transmission lines. The figure shows that the difference at 10 GHz for the microstrip (cpw micro), for smooth vs. rough copper, RMS = 0.4 vs. RMS = 2.8, respectively, is approximately 0.09 in terms of the effective dielectric constant. The same consideration for the tightly coupled CBCPW is approximately 0.06. Even though trapezoidal effects will cause

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**TABLE I**

<table>
<thead>
<tr>
<th>DIFFERENT CIRCUITS DIMENSIONS AND MEASURED CHARACTERISTIC IMPEDANCES</th>
<th>Nominal Circuit Dimensions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Measures Characteristic Impedance (Ohm)</td>
<td>Conductor Width (µm, mils)</td>
</tr>
<tr>
<td>RMS = 0.4 µm</td>
<td>RMS = 1.8 µm</td>
</tr>
<tr>
<td>Microstrip</td>
<td>51.2</td>
</tr>
<tr>
<td>CPW Launch Microstrip</td>
<td>50.2</td>
</tr>
<tr>
<td>CBCPW Tightly Coupled</td>
<td>47.1</td>
</tr>
<tr>
<td>CBCPW Moderate Coupled</td>
<td>50.6</td>
</tr>
<tr>
<td>CBCPW Loosely Coupled</td>
<td>50.8</td>
</tr>
</tbody>
</table>

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**Figure 3** Effective dielectric constant of a 4 mil LCP laminate with a 50 Ω microstrip line with different surface roughness.

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constant is much less for CBCPW than for microstrip. The figure also shows a difference in dispersion, where the effective dielectric constant will vary more with frequency for microstrip than for CBCPW. Trapezoidal effects are not considered in the data shown; however, CBCPW circuits could have slightly more dispersion than normal if trapezoidal effects are greater.

Figure 6 shows the insertion loss associated with the two different circuit types and with different copper surface roughnesses. At 10 GHz, the difference in loss for microstrip on rough copper versus smooth copper is approximately 0.250 dB/in. to 0.121 dB/in. For CBCPW, the difference is about 0.280 dB/in. to 0.167 dB/in. The insertion loss performance of CBCPW is less affected by copper surface roughness than the insertion loss performance of microstrip. Trapezoidal effects will have more influence on insertion loss performance for CBCPW than for microstrip.

**SIMULATIONS AND MEASUREMENTS**

To better understand the performance of the circuits studied in this article, models were constructed and analyzed with the help of Sonnet Suite Professional V13.54, a three-dimensional (3D) planar EM simulation software. Based on microsectional data from the circuits tested, the simulation geometries, such as substrate thickness and metal surface profile, were entered into the software. An optical coordinate measuring machine (CMM) was used to determine the circuit length accurately. Figure 7 shows an image of one of the CBCPW circuits as it appears in the Sonnet software, while Figure 8 shows a microphotograph of the corresponding cross-section of the circuit.

While Sonnet contains a native support for modeling thick metal, Figure 7 shows a thick metal approximation drawn manually using the software. Two infinitely thin metals were used in this model, separated by the physical thickness of the metal. The top-layer metal has a width equivalent to the top of the physical metal, and the bottom-layer metal has a width equivalent to the bottom. The layers are then connected with edge vias. This serves to effectively model the thickness of the metal as well as the CBCPW trapezoidal effects — the bottom metal can be seen protruding slightly past the edge via, providing the “sharpness” of the physical profile.

A key to achieving success in the simulation of these types of microstrip and CBCPW circuits is a recently introduced surface-roughness model to V13 of the Sonnet software. The model, which was developed by Sonnet Software’s software engineers in collaboration with Rogers’ material developers, represents a significant advance in metal profile modeling, accounting for the effects on surface inductance of current following partial “loops” in a metal conductor’s profile. While it is possible to use the new surface roughness model on the top and bottom of a PCB, it is only applied to the bottom surface of the bottom metal. Roughness is intentionally added only to this physical surface, to aid adhesion to the PCB dielectric material.

Figure 9 offers a comparison between a simulated model and the mea-
accuracy of the model and the method of experimental error, confirming the geometries, it is well within the limits is not as close as that for the microstrip measurements for CBCPW structures. While the difference between simulations and measurements provides reassurance of the test RMS) metal surfaces. This close agreement (0.4 µm RMS) and rough (2.8 µm was achieved between the simulated diredths of decibels, good agreement conditions. Both measurements and computer simulations were performed using a commercial, low-loss microwave substrate material with different copper types, including different values of copper conductor surface roughness. The effects of copper surface roughness were evaluated and compared, showing that greater roughness typically means greater loss. Different circuit topologies were compared through both measurements and simulations and, by properly applying computer simulation software, it is possible to reduce the difficulties often encountered with lesser-known circuit topologies.

Fig. 11 CBCPW geometry can be broken into three key parameters.

Fig. 12 Example of a “parameter sweep” simulation.

<table>
<thead>
<tr>
<th>Fig. 9 Simulated and measured microstrip insertion loss.</th>
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<tr>
<td><img src="image9.png" alt="Image" /></td>
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<thead>
<tr>
<th>Fig. 10 Simulated and measured CBCPW insertion loss.</th>
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<th>Fig. 12 Example of a “parameter sweep” simulation.</th>
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</table>

Having established the validity of the surface roughness simulations, it might be beneficial to see how they can be further used in high-frequency circuit design. For example, a common issue with circuit topologies like CBCPW is finding the desired impedance. While many textbook formulas are available for this purpose for conventional microstrip circuits, it is less true for CBCPW circuits. Fortunately, EM simulators are suitable for finding CBCPW geometries for the desired impedance for nearly any reasonable circuit topology. The impedance of a CBCPW design for any PCB material can be broken down to three main parameters: conductor width, material thickness and ground plane separation. As Figure 11 shows, the effects of each of these parameters on CBCPW transmission-line impedance can then be readily analyzed within the EM simulator environment.

Once parameterization is complete, a simulation can be run, which automatically “sweeps” all combinations of the three parameters within a desired range. It is then convenient to plot all impedances on the same graph, allowing a designer to choose the best geometry and impedance from the results. Figure 12 shows an example of such an impedance plot.

**ConCLuSion**

The performance levels of microstrip, CBCPW launched microstrip and CBCPW transmission lines were evaluated under controlled conditions. Both measurements and computer simulations were performed using a commercial, low-loss microwave substrate material with different copper types, including different values of copper conductor surface roughness. The effects of copper surface roughness were evaluated and compared, showing that greater roughness typically means greater loss. Different circuit topologies were compared through both measurements and simulations and, by properly applying computer simulation software, it is possible to reduce the difficulties often encountered with lesser-known circuit topologies.

**References**


2. R.N. Simons, “Coplanar Waveguide Circuits and EM simulators were compared through both measurements and simulations and, by properly applying computer simulation software, it is possible to reduce the difficulties often encountered with lesser-known circuit topologies.


**Technical Feature**

**Figures**

- Fig. 9: Simulated and measured microstrip insertion loss.
- Fig. 10: Simulated and measured CBCPW insertion loss.
- Fig. 11: CBCPW geometry can be broken into three key parameters.
- Fig. 12: Example of a “parameter sweep” simulation.